



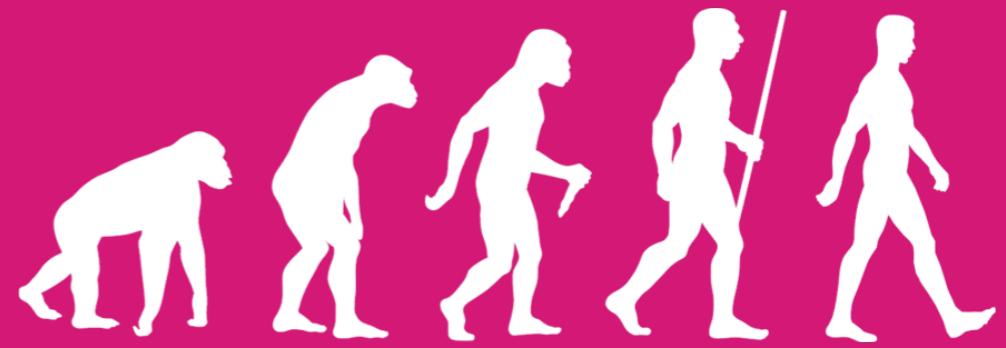
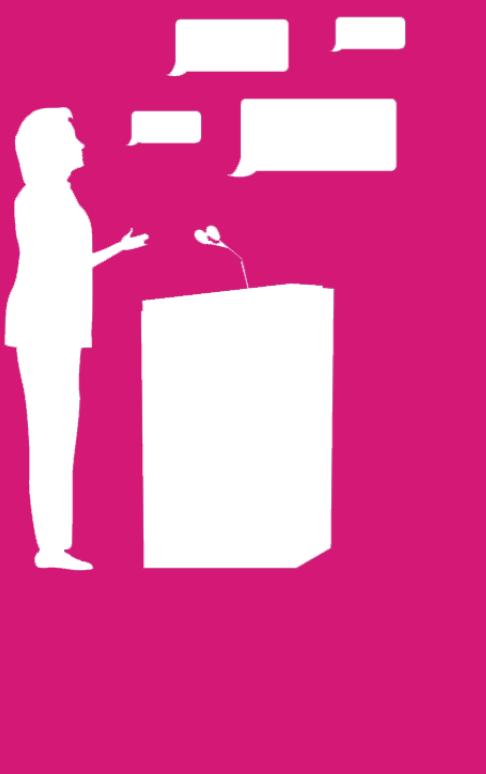
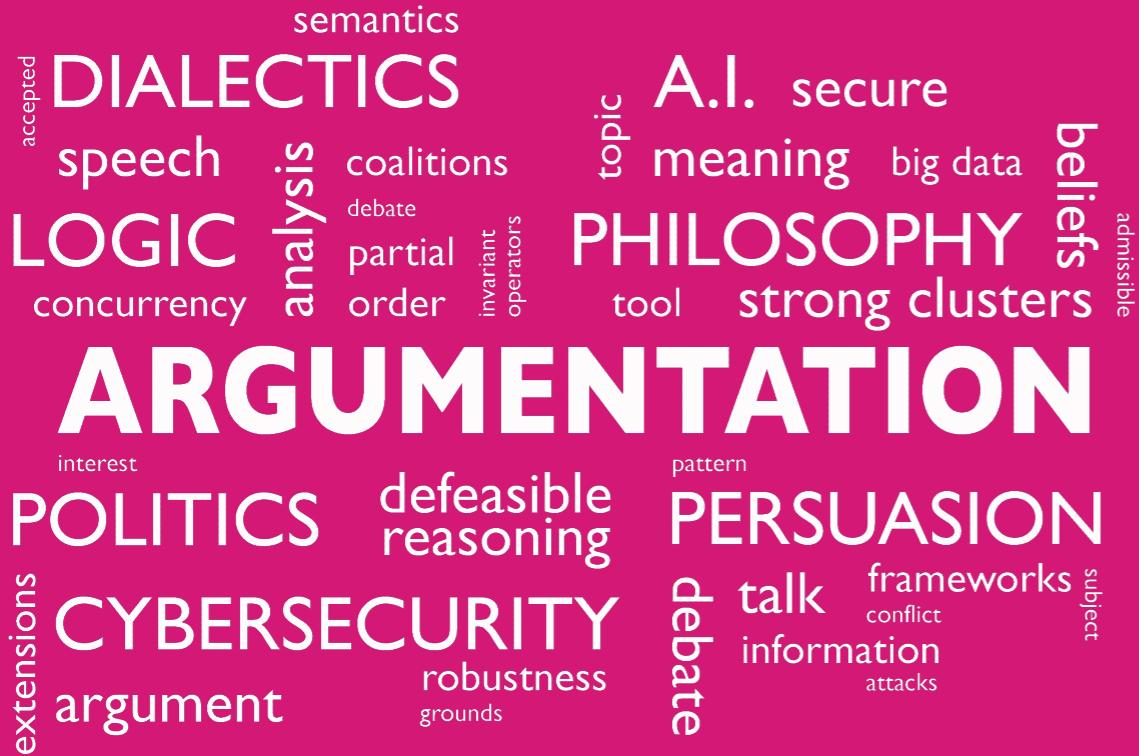
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# Timed Concurrent Language for Argumentation

**Stefano Bistarelli, Maria Chiara Meo, Carlo Taticchi**

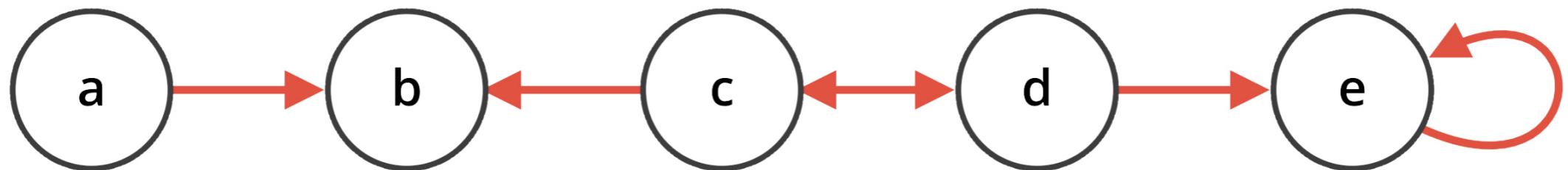
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# Overview

- Argumentation Frameworks (AFs)
  - Acceptable arguments
  - Timed AFs
- Timed Concurrent Language for Argumentation (tcl<sub>a</sub>)
  - Syntax
  - Operational semantics
- Modelling Timed AFs
  - Running example
- Conclusion and Future Work

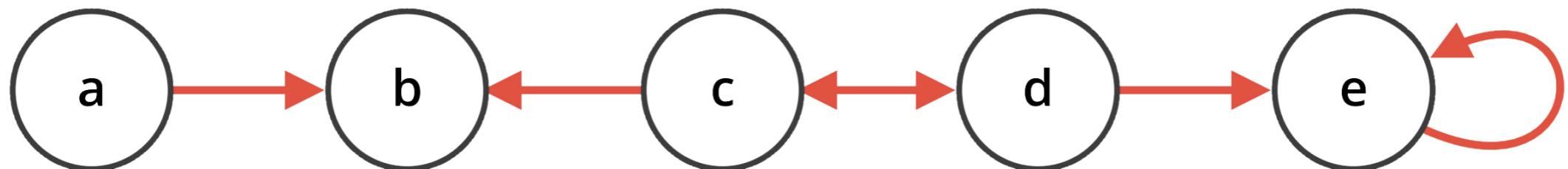
# Argumentation Frameworks



# Argumentation Frameworks

## Acceptable arguments

- Conflict-Free: {}, {a}, {b}, {c}, {d}, {a,c}, {a,d}, {b,d}
- Admissible: {}, {a}, {b}, {c}, {d}, {a,c}, {a,d}, {b,d}
- Complete: {}, {a}, {b}, {c}, {d}, {a,c}, {a,d}, {b,d}
- ...



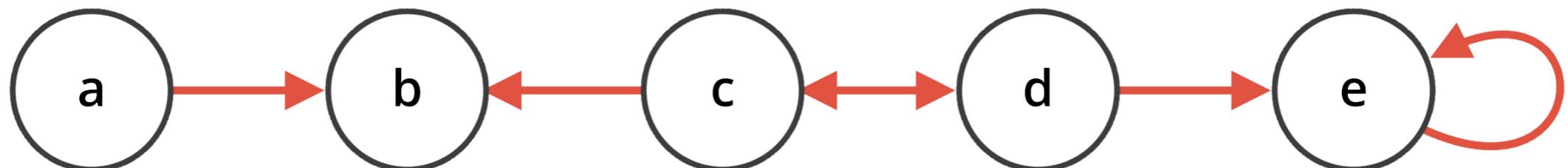
Extension-based semantics

# Argumentation Frameworks

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- Admissible: {}, {a}, {b}, {c}, {d}, {a,c}, {a,d}, {b,d}
- Complete: {}, {a}, {b}, {c}, {d}, {a,c}, {a,d}, {b,d}
- ...

Credulously accepted

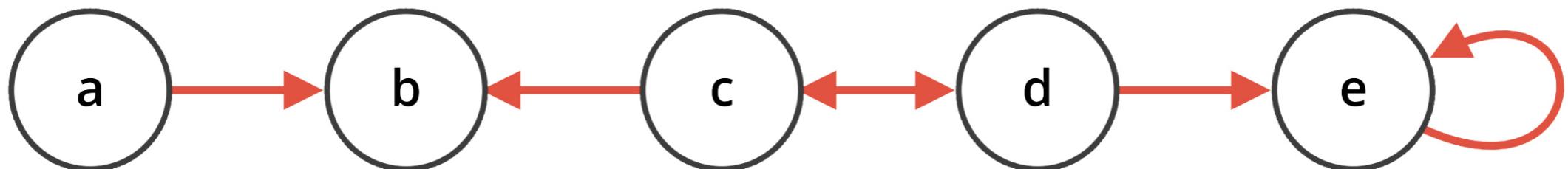


Extension-based semantics

# Argumentation Frameworks

## Acceptable arguments

- Conflict-Free: {}, {a}, {b}, {c}, {d}, {a,c}, {a,d}, {b,d}
- Admissible: {}, {a}, {b}, {c}, {d}, {a,c}, {a,d}, {b,d}
- Complete: {}, **{a}**, {b}, {c}, {d}, **{a,c}**, **{a,d}**, {b,d}
- ...      **Skeptically accepted**      **Credulously accepted**



**Extension-based semantics**

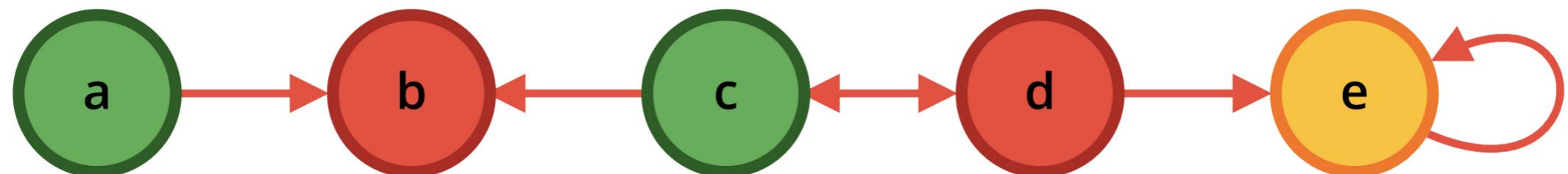
# Argumentation Frameworks

## Acceptable arguments

**IN** if it is attacked only by **OUT** arguments

**OUT** if it is attacked by at least an **IN** argument

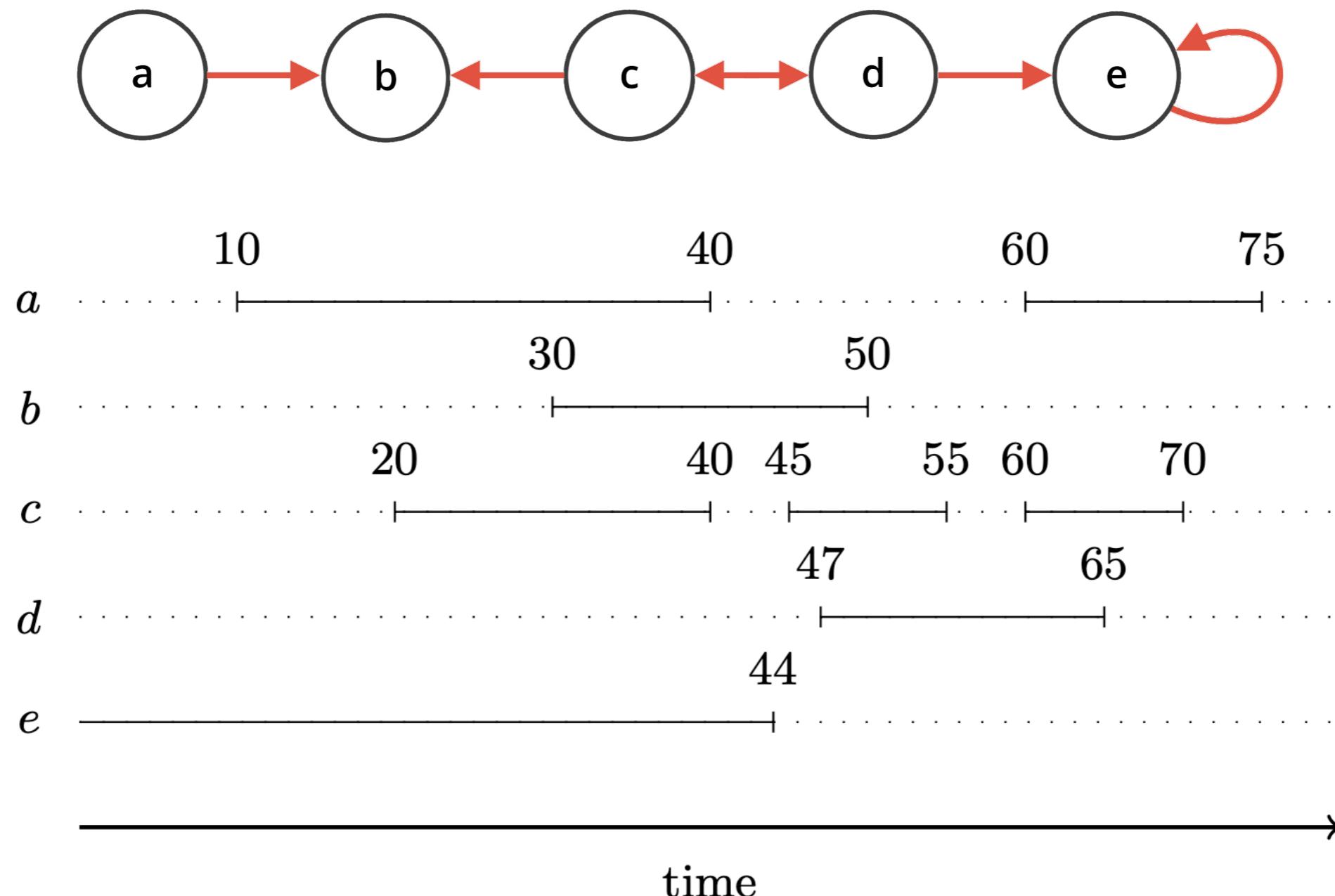
**UNDEC** otherwise



**Reinstatement labelling identifies complete extensions**

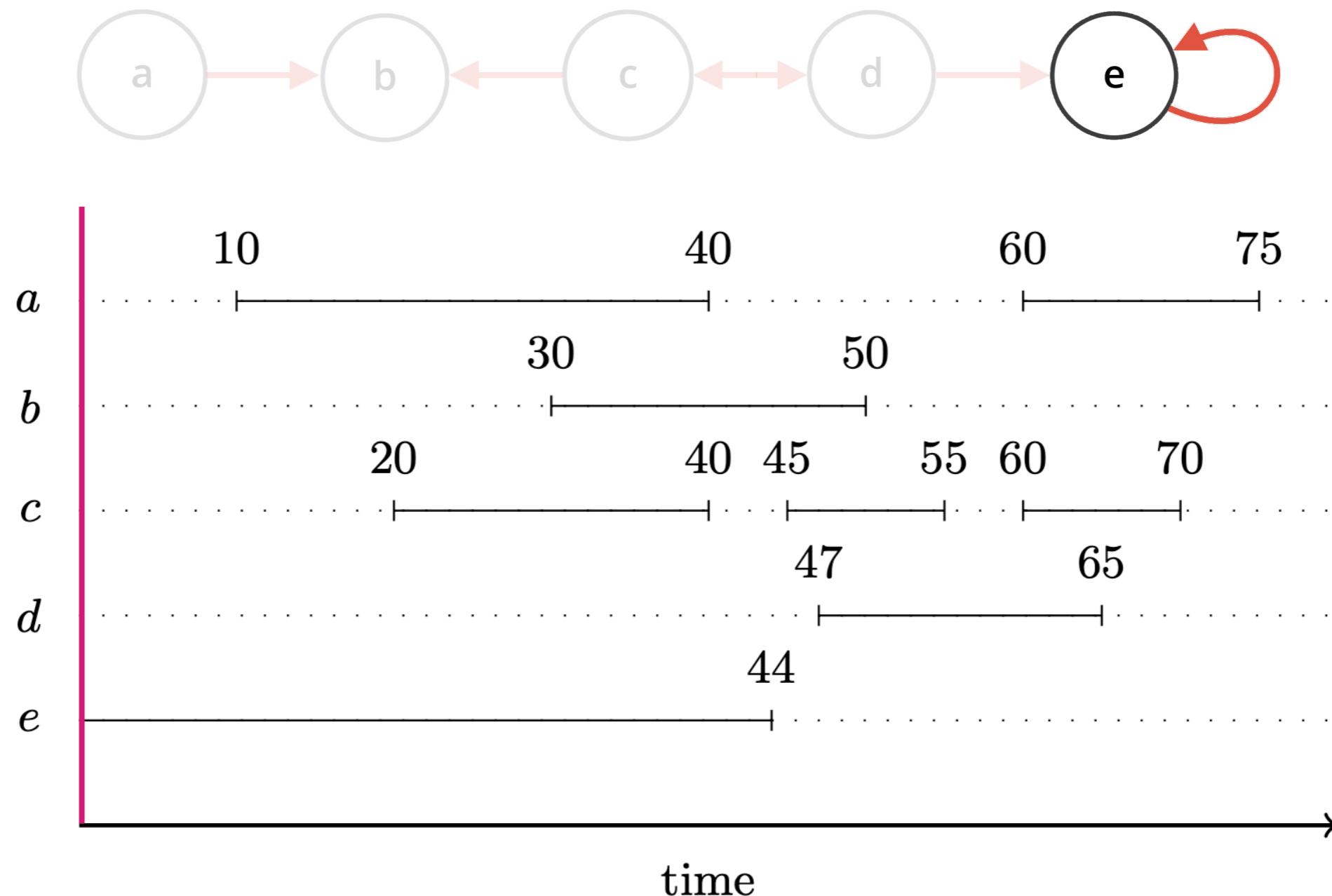
# Argumentation Frameworks

## Timed AFs



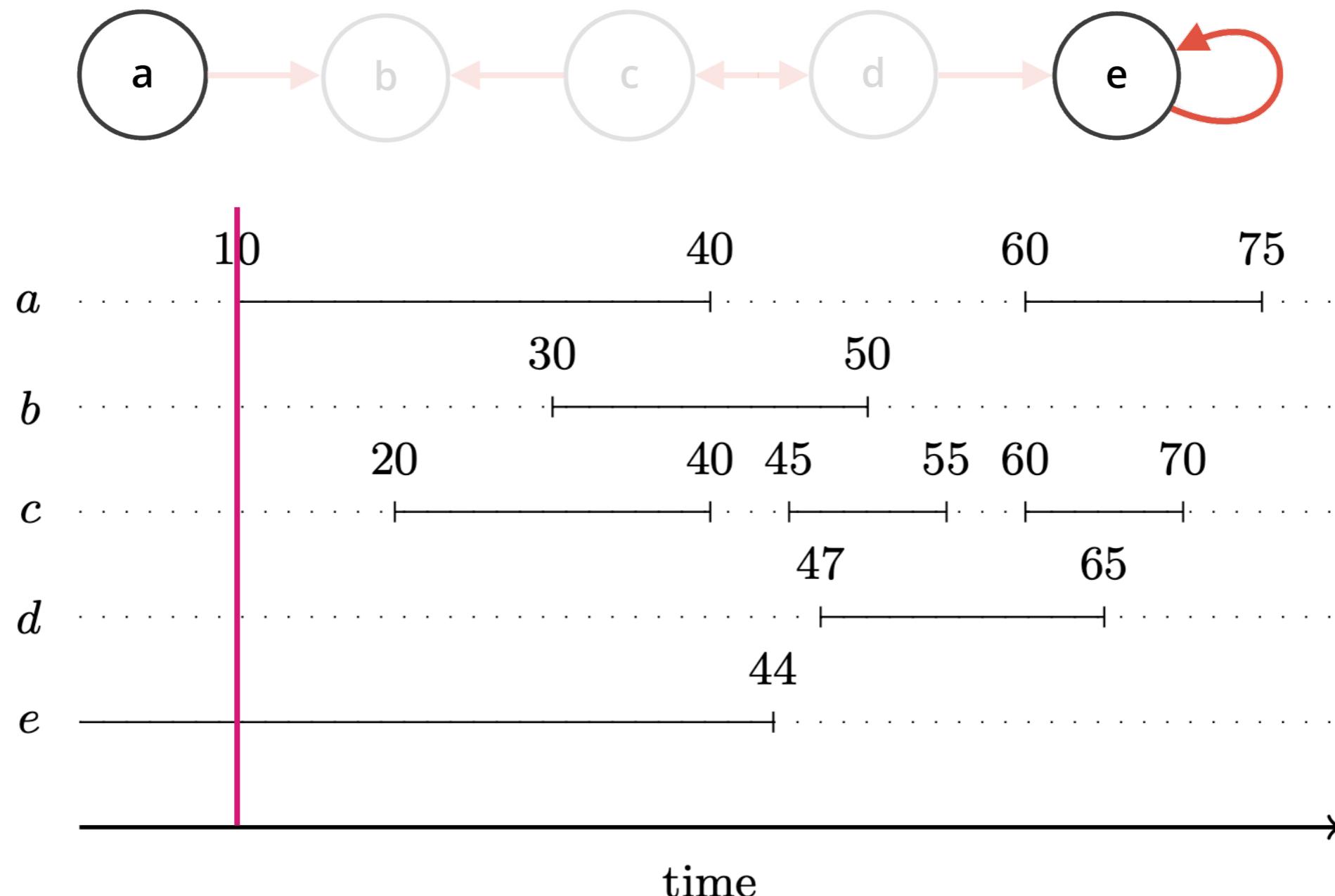
# Argumentation Frameworks

## Timed AFs



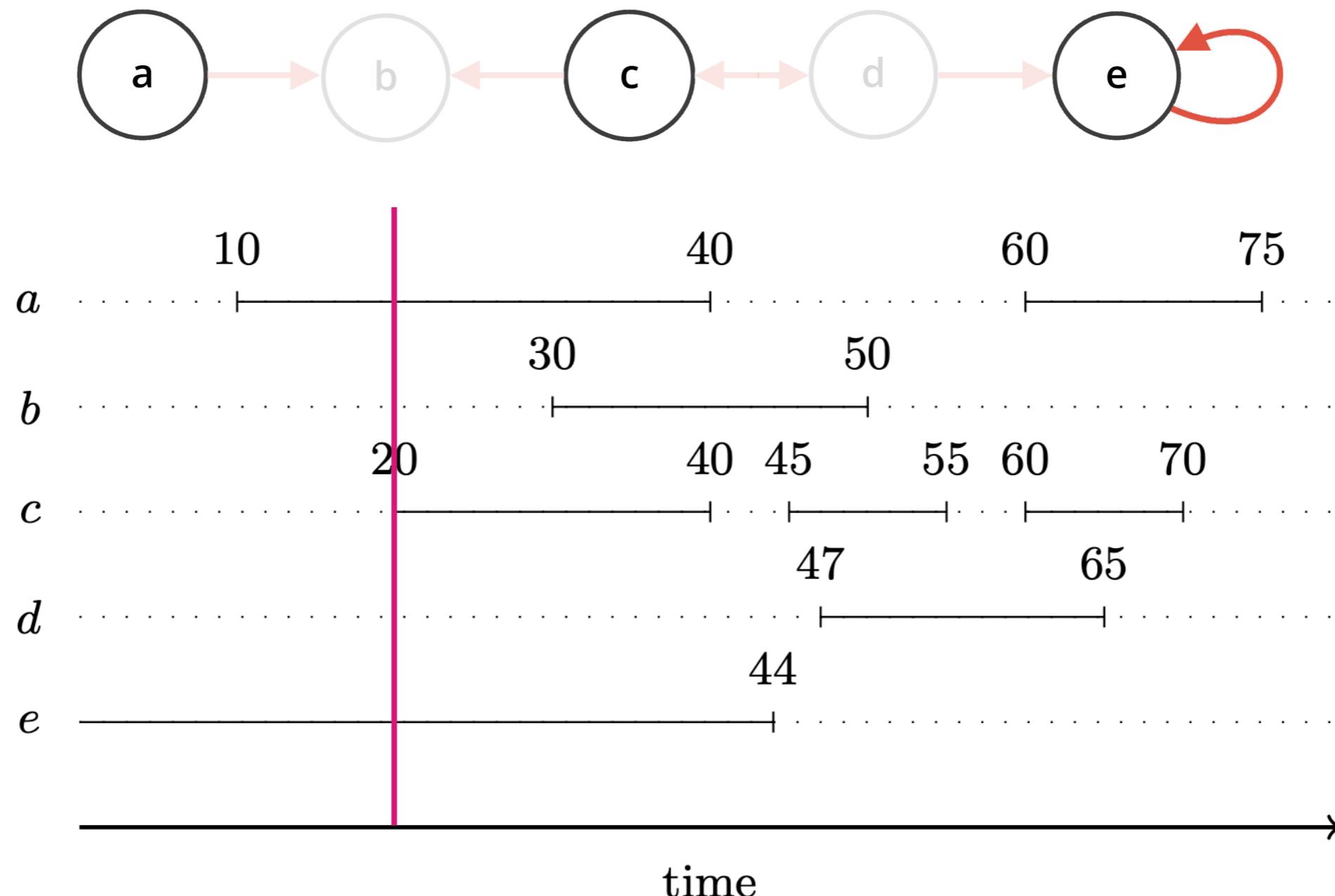
# Argumentation Frameworks

## Timed AFs



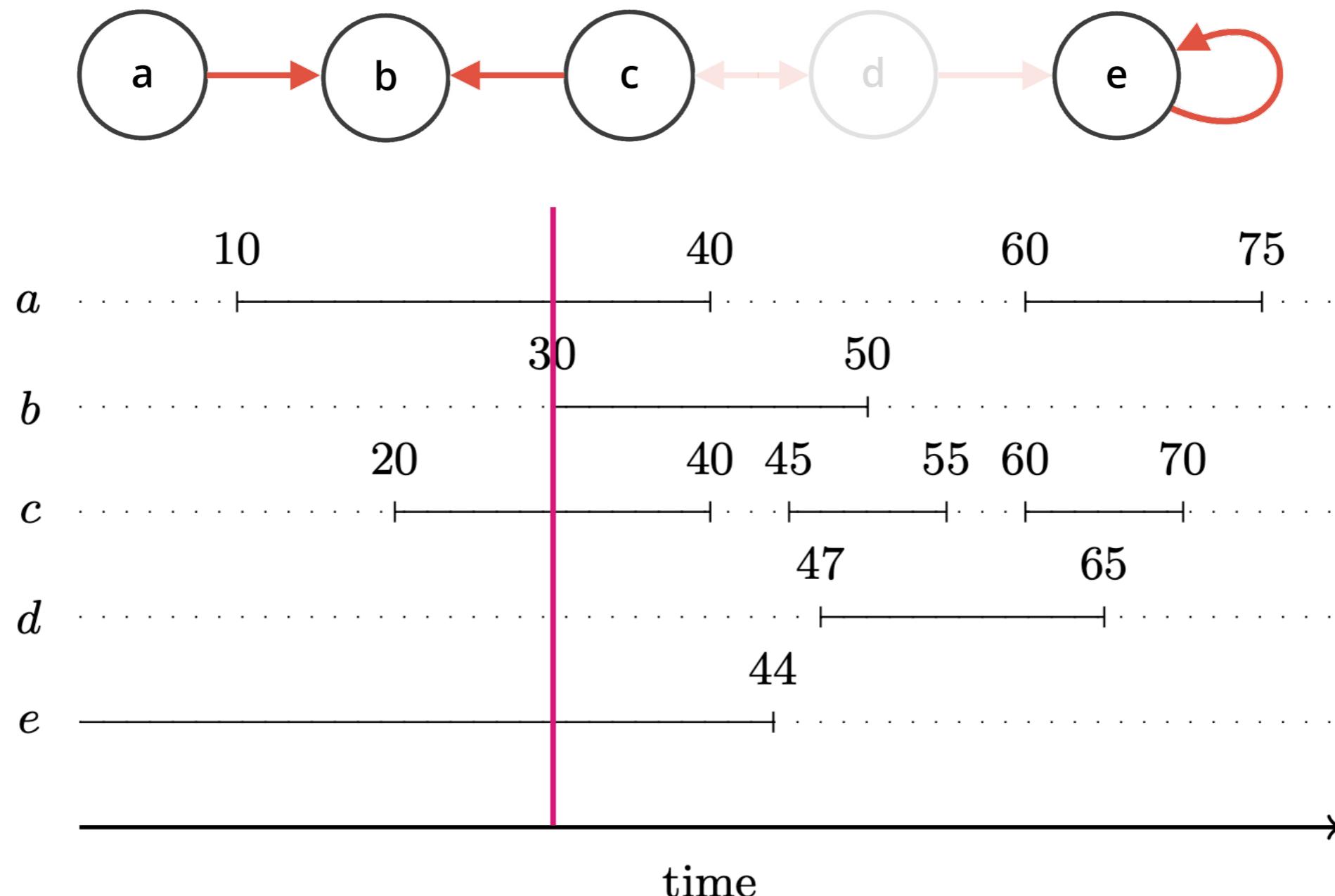
# Argumentation Frameworks

## Timed AFs



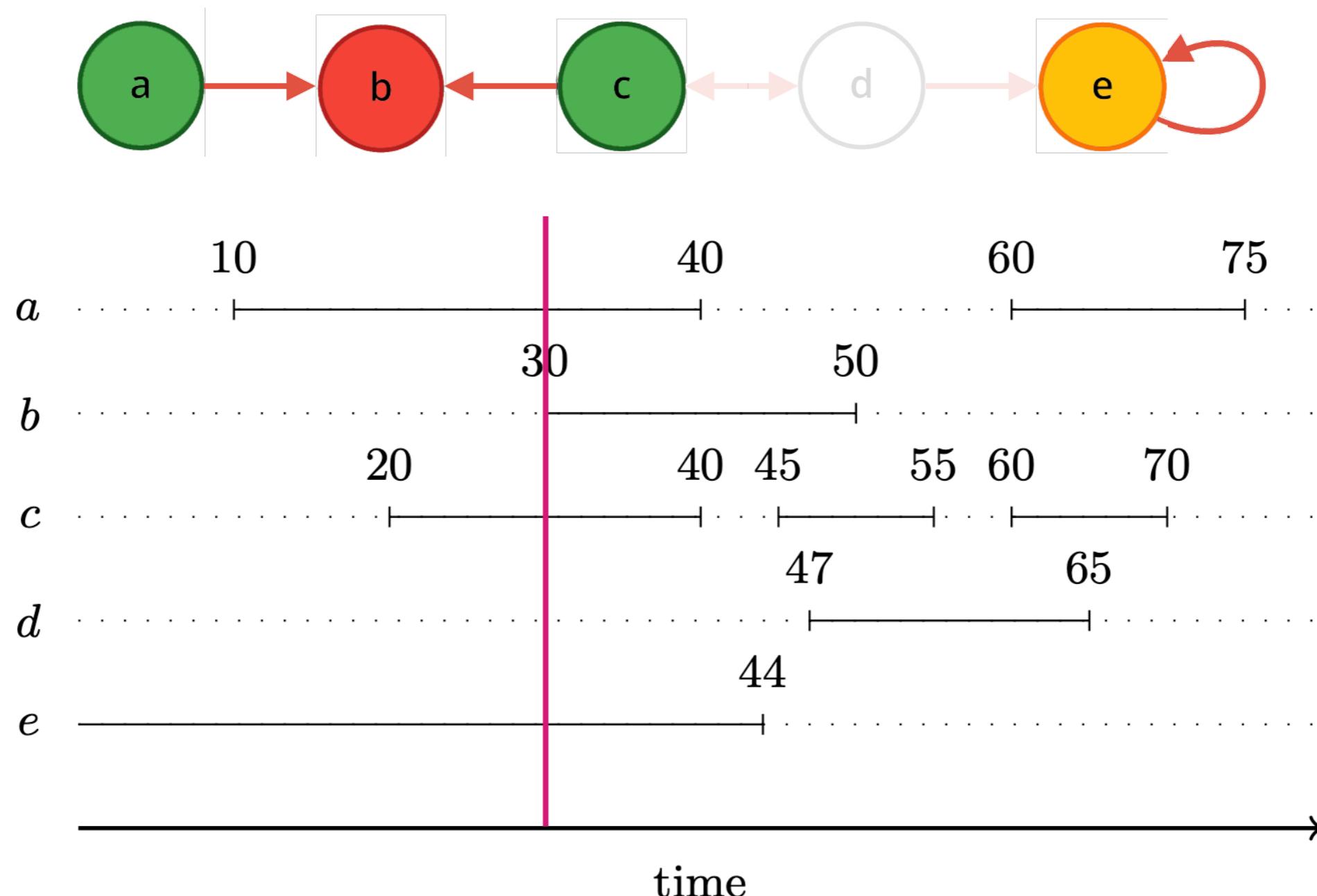
# Argumentation Frameworks

## Timed AFs



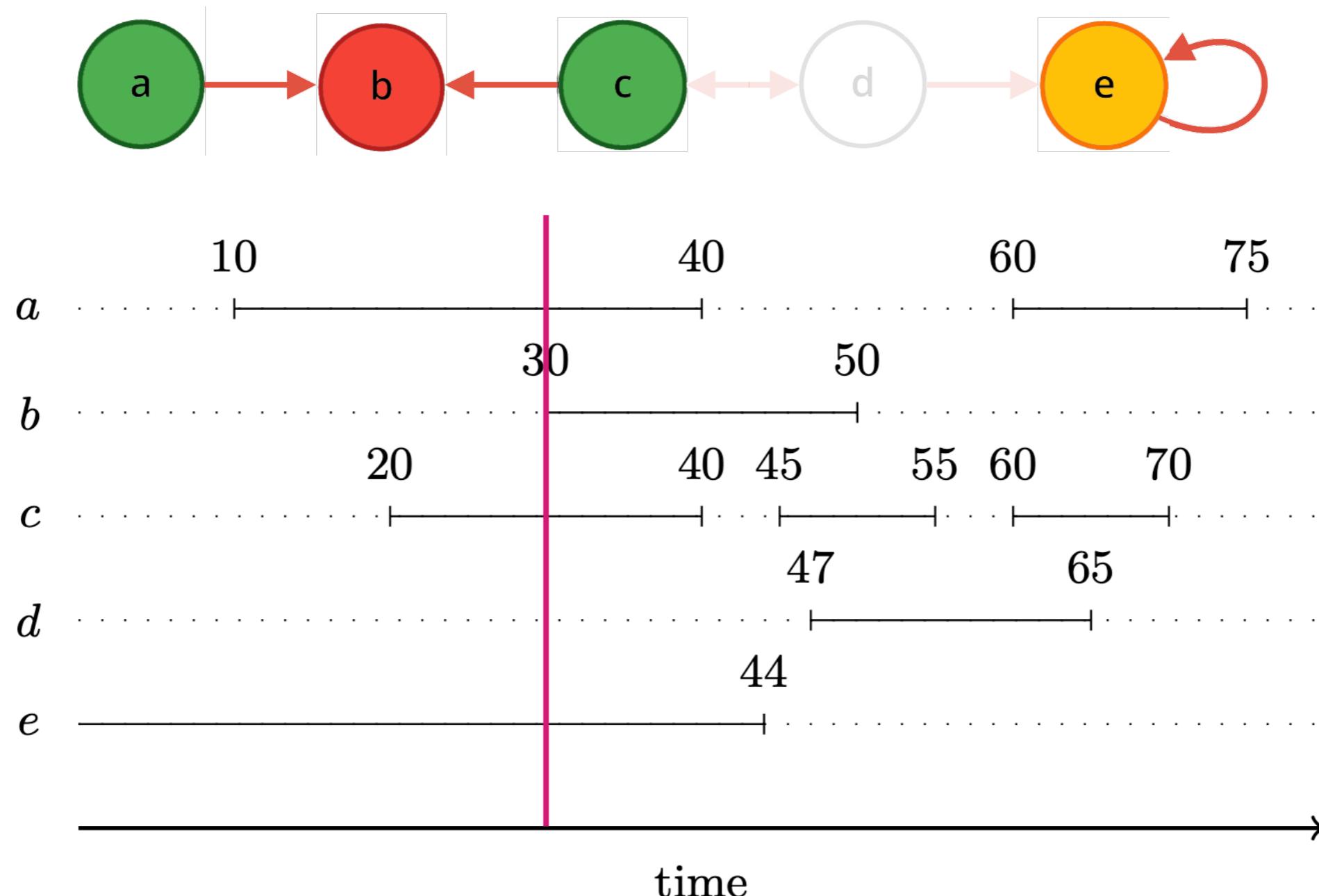
# Argumentation Frameworks

## Timed AFs



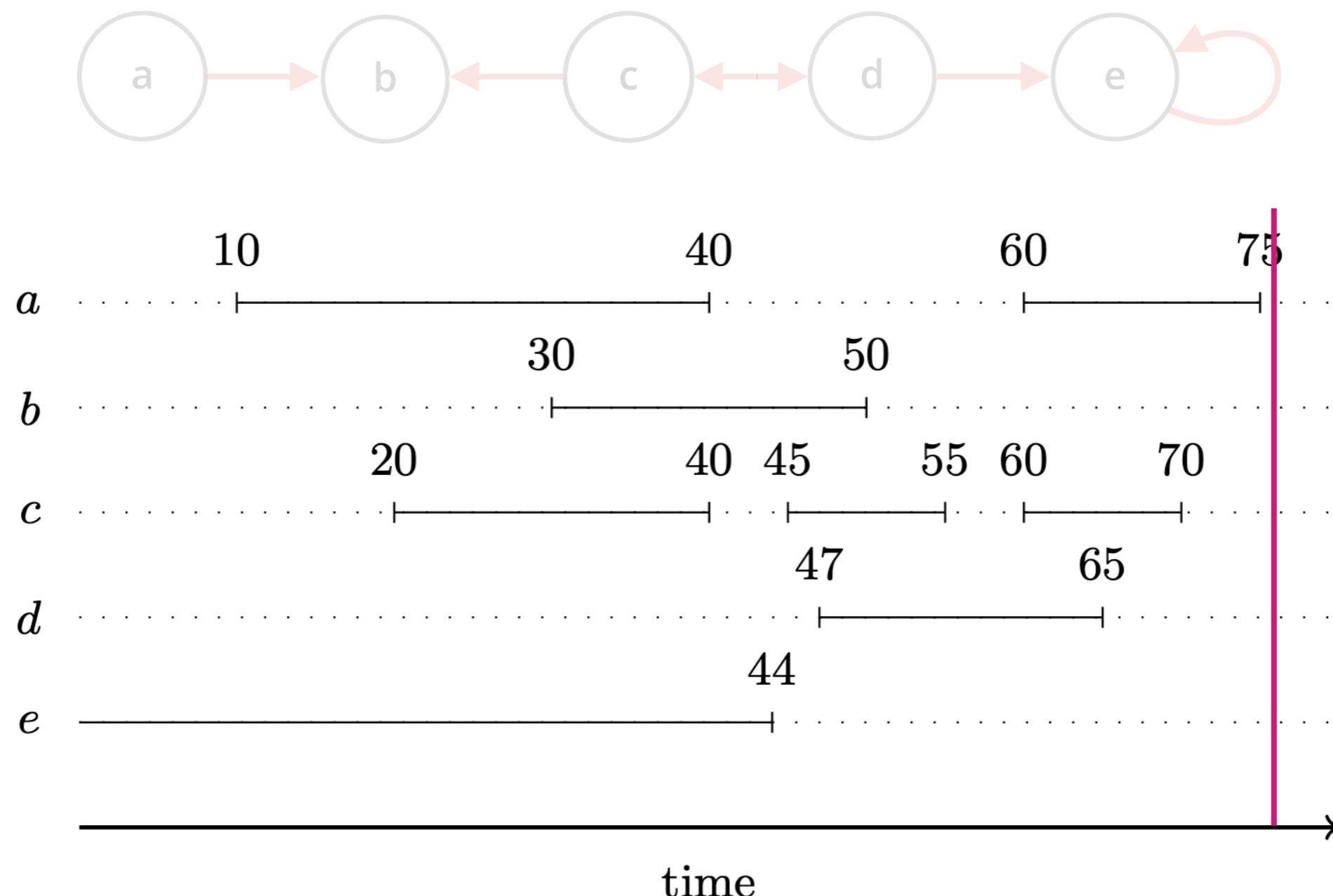
# Argumentation Frameworks

## Timed AFs



# Argumentation Frameworks

## Timed AFs



# Timed Concurrent Language for Argumentation

## Syntax

- Models concurrent processes taking place over time
  - Knowledge base represented through AFs
  - Bounded asynchrony and maximal parallelism
- 
- $A ::= success \mid failure \mid add(Arg, R) \rightarrow A \mid rmv(Arg, R) \rightarrow A$   
   $\mid A \parallel A \mid \exists_x A \mid E \mid p(a, l, \sigma, i)$
  - $E ::= test_{c,t}(a, l, \sigma) \rightarrow A \mid test_{s,t}(a, l, \sigma) \rightarrow A \mid check_t(Arg, R) \rightarrow A$   
   $\mid E + E \mid E +_P E \mid E \parallel_G E$

# Timed Concurrent Language for Argumentation

## Operational Semantics (1)

$$\langle add(Arg', R') \rightarrow A, \langle Arg, R \rangle \rangle \longrightarrow \langle A, \langle Arg \cup Arg', R \cup R'' \rangle \rangle \quad \text{Add}$$

where  $R'' = \{(a, b) \in R' \mid a, b \in Arg \cup Arg'\}$

$$\langle rmv(Arg', R') \rightarrow A, \langle Arg, R \rangle \rangle \longrightarrow \langle A, \langle Arg \setminus Arg', R \setminus \{R' \cup R''\} \rangle \rangle \quad \text{Rmv}$$

where  $R'' = \{(a, b) \in R \mid a \in Arg' \vee b \in Arg'\}$

$$\frac{Arg' \subseteq Arg \wedge R' \subseteq R \quad t > 0}{\langle check_t(Arg', R') \rightarrow A, \langle Arg, R \rangle \rangle \longrightarrow \langle A, \langle Arg, R \rangle \rangle} \quad \text{Ch (1)}$$

$$\frac{Arg' \not\subseteq Arg \vee R' \not\subseteq R \quad t > 0}{\langle check_t(Arg', R') \rightarrow A, \langle Arg, R \rangle \rangle \longrightarrow \langle check_{t-1}(Arg', R') \rightarrow A, \langle Arg, R \rangle \rangle} \quad \text{Ch (2)}$$

$$\langle check_0(Arg', R') \rightarrow A, F \rangle \longrightarrow \langle failure, F \rangle \quad \text{Ch (3)}$$

# Timed Concurrent Language for Argumentation

## Operational Semantics (2)

$$\frac{\exists L \in S_\sigma(F) \mid l \in L(a) \quad t > 0}{\langle test_{c,t}(a, l, \sigma) \rightarrow A, F \rangle \longrightarrow \langle A, F \rangle} \quad \text{CT (1)}$$

$$\frac{\forall L \in S_\sigma(F).l \notin L(a) \quad t > 0}{\langle test_{c,t}(a, l, \sigma) \rightarrow A, F \rangle \longrightarrow \langle test_{c,t-1}(a, l, \sigma) \rightarrow A, F \rangle} \quad \text{CT (2)}$$

$$\langle test_{c,0}(a, l, \sigma) \rightarrow A, F \rangle \longrightarrow \langle failure, F \rangle \quad \text{CT (3)}$$

$$\frac{\forall L \in S_\sigma(F).l \in L(a) \quad t > 0}{\langle test_{s,t}(a, l, \sigma) \rightarrow A, F \rangle \longrightarrow \langle A, F \rangle} \quad \text{ST (1)}$$

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$$\langle test_{s,0}(a, l, \sigma) \rightarrow A, F \rangle \longrightarrow \langle failure, F \rangle \quad \text{ST (3)}$$

# Timed Concurrent Language for Argumentation

## Operational Semantics (3)

$$\frac{\langle A_1, F \rangle \rightarrow \langle A'_1, F' \rangle, \quad \langle A_2, F \rangle \rightarrow \langle A'_2, F'' \rangle}{\langle A_1 \| A_2, F \rangle \rightarrow \langle A'_1 \| A'_2, * (F, F', F'') \rangle} \quad \text{Pa}$$

$$\frac{\langle E_1, F \rangle \rightarrow \langle A_1, F \rangle, \quad \langle E_2, F \rangle \rightarrow \langle A_2, F \rangle, \quad E_1, E_2 \notin \mathcal{E}_0, \quad A_1 \notin \mathcal{E}}{\langle E_1 \|_G E_2, F \rangle \rightarrow \langle A_1 \| A_2, F \rangle} \quad \text{GP (1)}$$

$$\frac{\langle E_1, F \rangle \rightarrow \langle E'_1, F \rangle, \quad \langle E_2, F \rangle \rightarrow \langle E'_2, F \rangle, \quad E_1, E_2 \notin \mathcal{E}_0, \quad E'_1, E'_2 \in \mathcal{E}}{\langle E_1 \|_G E_2, F \rangle \rightarrow \langle E'_1 \|_G E'_2, F \rangle} \quad \text{GP (2)}$$

$$\frac{E_1 \in \mathcal{E}_0, \langle E_2, F \rangle \rightarrow \langle A_2, F \rangle}{\langle E_1 \|_G E_2, F \rangle \rightarrow \langle A_2, F \rangle} \quad \text{GP (3)}$$

# Timed Concurrent Language for Argumentation

## Operational Semantics (4)

$$\frac{\langle E_1, F \rangle \rightarrow \langle A_1, F \rangle, \quad E_1 \notin \mathcal{E}_0, \quad A_1 \notin \mathcal{E}}{\langle E_1 + E_2, F \rangle \rightarrow \langle A_1, F \rangle} \quad \frac{E_1 \in \mathcal{E}_0, \langle E_2, F \rangle \rightarrow \langle A_2, F \rangle}{\langle E_1 + E_2, F \rangle \rightarrow \langle A_2, F \rangle} \text{ ND (1)}$$

$$\frac{\langle E_1, F \rangle \rightarrow \langle E'_1, F \rangle, \quad \langle E_2, F \rangle \rightarrow \langle E'_2, F \rangle, \quad E_1, E_2 \notin \mathcal{E}_0, \quad E'_1, E'_2 \in \mathcal{E}}{\langle E_1 + E_2, F \rangle \rightarrow \langle E'_1 + E'_2, F \rangle} \text{ ND (2)}$$

$$\frac{\langle E_1, F \rangle \rightarrow \langle A_1, F \rangle, \quad E_1 \notin \mathcal{E}_0, \quad A_1 \notin \mathcal{E}}{\langle E_1 +_P E_2, F \rangle \rightarrow \langle A_1, F \rangle} \quad \text{If (1)}$$

$$\frac{\langle E_1, F \rangle \rightarrow \langle E'_1, F \rangle, \quad E_1 \notin \mathcal{E}_0, \quad E'_1 \in \mathcal{E}}{\langle E_1 +_P E_2, F \rangle \rightarrow \langle E'_1 +_P E_2, F \rangle} \quad \frac{E_1 \in \mathcal{E}_0, \langle E_2, F \rangle \rightarrow \langle A_2, F \rangle}{\langle E_1 +_P E_2, F \rangle \rightarrow \langle A_2, F \rangle} \quad \text{If (2)}$$

# Modelling Timed AFs

## Example

- Each agent handles one argument
- Agent\_a:  $sleep(9) \rightarrow (add(\{a\}, \{(b, a), (d, a)\}) \rightarrow (sleep(30) \rightarrow (rmv(\{a\}, \{\}) \rightarrow (sleep(18) \rightarrow (add(\{a\}, \{(b, a), (d, a)\}) \rightarrow (sleep(15) \rightarrow (rmv(\{a\}, \{\}) \rightarrow success)))))))$
- Agent\_b:  $sleep(29) \rightarrow (add(\{b\}, \{(b, a), (c, b)\}) \rightarrow (sleep(20) \rightarrow (rmv(\{b\}, \{\}) \rightarrow success)))$
- Agent\_a || Agent\_b

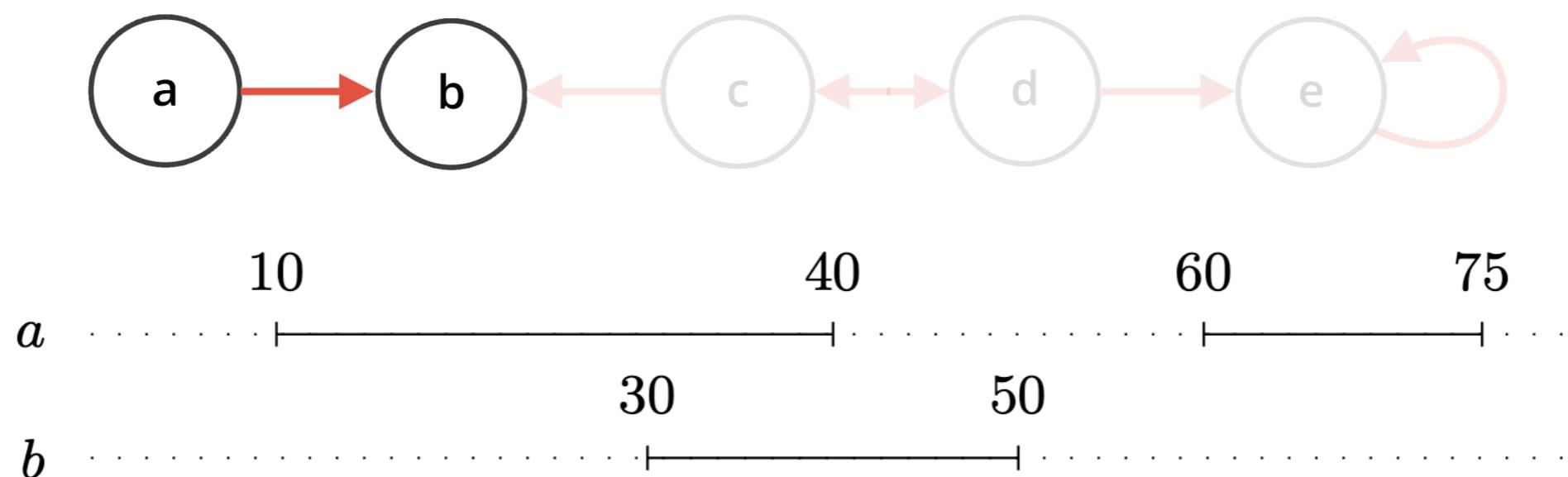
$sleep(t) \rightarrow A$  is a shortcut for

$$\begin{cases} A & \text{if } t \leq 0 \\ check_1(\{\}, \{\}) \rightarrow (sleep(t - 1) \rightarrow A) & \text{otherwise} \end{cases}$$

# Modelling Timed AFs

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- Agent\_b:  $sleep(29) \rightarrow (add(\{b\}, \{(b, a), (c, b)\}) \rightarrow (sleep(20) \rightarrow (rmv(\{b\}, \{\}) \rightarrow success)))$
- Agent\_a || Agent\_b



# tcla Web Interface

- <http://conarg.dmi.unipg.it/tcla>
- Run all / step-by-step execution
- Shows program output + shared memory status + Timed AF

**Input Program (write or select [Example 5]):**

```
add({a,b}, {(a,b)}) -> testc({a}, in, admissible, 2) -> add({v}, {}) -> success;
```

**Program Output:**

```
1 ----- level 0 -----
2 prg: add({a,b}, {(a,b)})->testc({a}, in, admissible, 2)->add({v}, {})->success;
3 ----- level 1 -----
4 par: add({a,b}, {(a,b)})->testc({a}, in, admissible, 2)->add({v}, {})->success
5 ----- level 2 -----
6 add: add({a,b}, {(a,b)})->testc({a}, in, admissible, 2)->add({v}, {})->success
7 ----- level 3 -----
8 tcr: testc({a}, in, admissible, 2)->add({v}, {})->success
9 Credulous Test succeeded
10 ----- level 4 -----
11 add: add({v}, {})->success
12 ----- level 5 -----
13 suc: success
14 ----- level 6 -----
15 SUCCESS
```

**Shared Memory:**

```
arg(a).
arg(b).
att(a,b).
arg(v).
```

**Timed AF:**

2	3	4	5	6
a	[Blue Bar]			
b	[Light Blue Bar]			
v	[Orange Bar]			

# Conclusion

- tcla models concurrent argumentation processes over time

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- We showed how to translate Timed AFs into `tcla` processes
  - ▶ the arguments in the store at time  $t$  are all and only the arguments available at  $t$  in the original Timed AF
  - ▶ the set of accepted arguments in the store at  $t$  coincides with the set of extensions at  $t$  in the original Timed AF

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- Working implementation available online

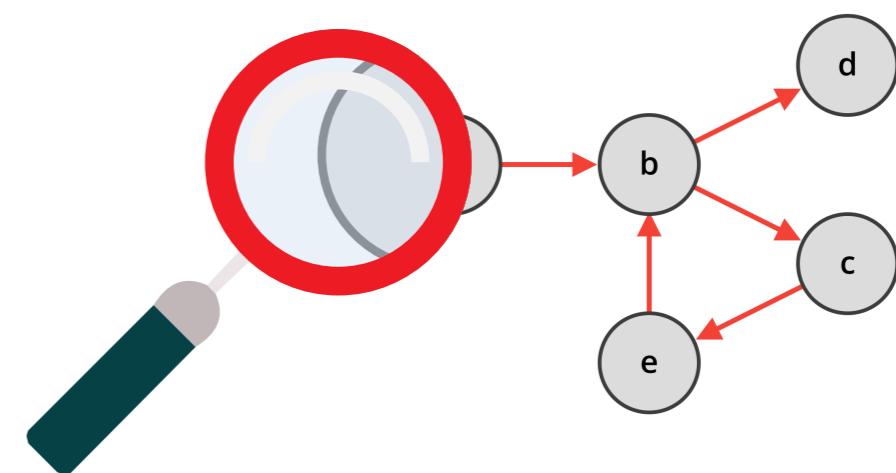
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**... `tcla` can do more than just modelling Timed AFs!**

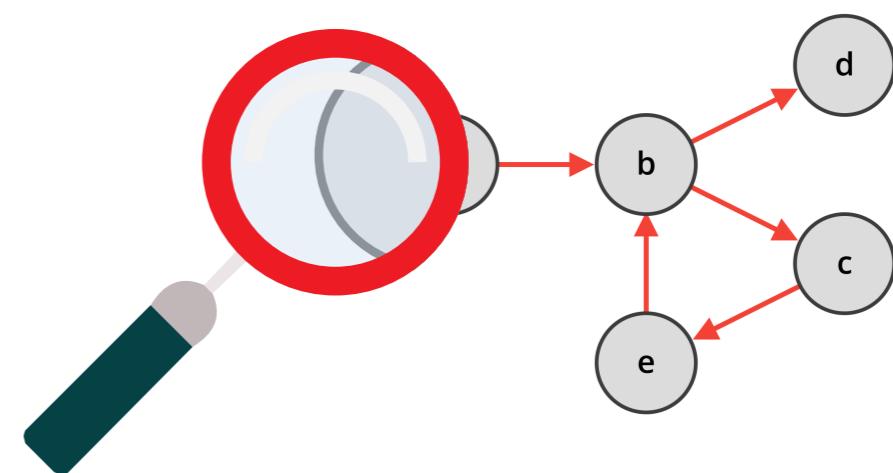
# Future Work

- Negotiation/debating/persuasion between agents



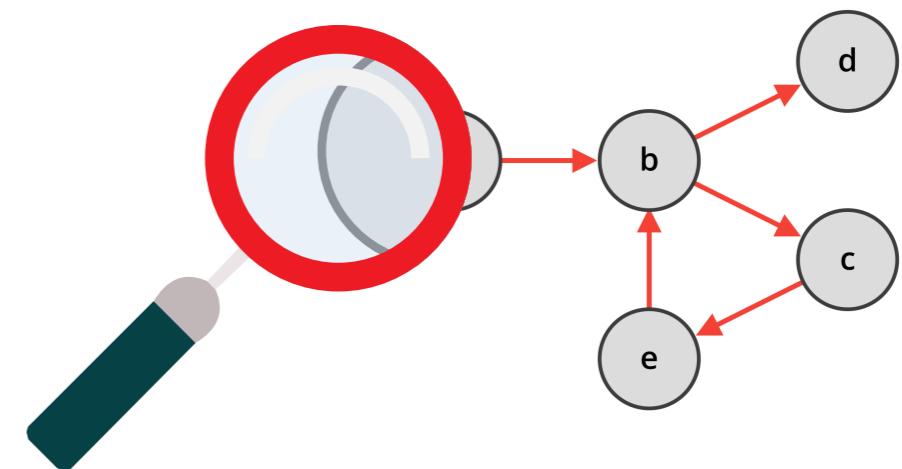
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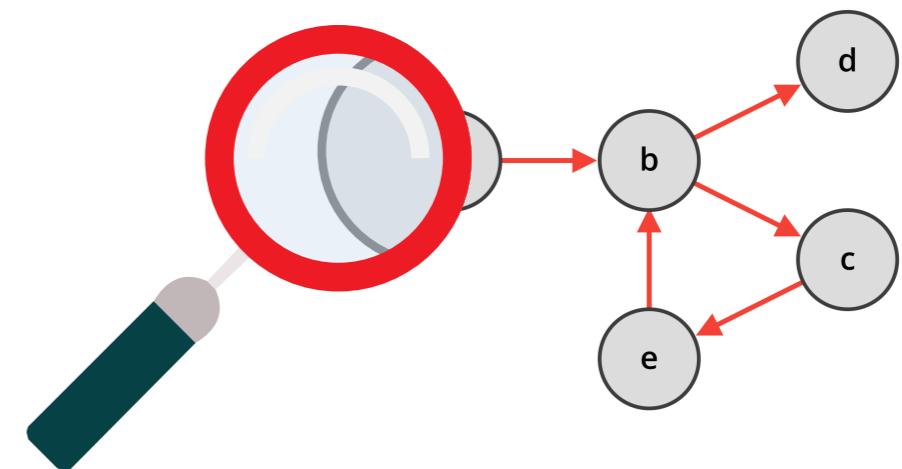
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- Study time-dependent notions of acceptability



# Future Work

- Negotiation/debating/persuasion between agents
- Use interleaving instead of maximal parallelism for time passing
- Study time-dependent notions of acceptability
- Connections with the AGM Framework



# Thank you for your attention!



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